

Lab 4 – Exercise on Filter Techniques in Frequency Domain

**Problem 1: Exercises on Low-pass and High-pass Filters in the Frequency Domain**

- a) Design a butterworth low-pass filter of order 2 with a cutoff frequency of 80 in the frequency domain. Obtain the filtered image by filtering the original image *Sample* with the designed butterworth filter. Display the original image, the butterworth low-pass filter (**treat it as an image**), and the filtered image in figure 1 with the appropriate titles.
- b) Repeat the step a) by using the corresponding high-pass filter. Display the corresponding images (original image, high-pass filter, and filtered image) in figure 2 with the appropriate titles.
- c) Close all figures and all variables in the workspace.

**Problem 2: Remove Additive Cosine Noise**

The noisy image *boy\_noisy.gif* has been generated by adding some noise in the form of a cosine function. Your goal is to remove the cosine interference. This can be done as follows:

- a) Compute the centered DFT of the noisy image.
- b) Compute the magnitude and find the frequencies corresponding to the *four largest distinct magnitudes* (do not consider the magnitude at the center – a very large value)
- c) Replace the value of each of the four frequencies, which correspond to the four largest distinct magnitudes, by the average of its 8 neighbors. (Make sure you will perform this change on their symmetric points to ensure the proper reconstruction).
- d) Take the inverse DFT transform and display the original image and the resulted image side-by-side in figure 1 with the appropriate titles.
- e) Explain why the four largest distinct values of the magnitude were chosen to do the processing via Matlab display command.
- f) Close all figures and variables in the workspace.

**Problem 3: Preliminary Wavelet Transform**

- a) Apply a maximum-level “db2” wavelet decomposition on *Lena* by using appropriate Matlab function(s). **You need to compute the maximum decomposition level instead of hard coding it.** Apply the inverse wavelet transform to restore the image. Use “if-else” statement to compare your restored image with the original image so the appropriate message indicating the equality or inequality between these two images should be displayed. (Note: The original image and the restored image should be the same)
- b) Apply a 4-level “db2” wavelet decomposition on *Lena* by using appropriate Matlab function(s). **Independently** perform the inverse wavelet transform after each of the following operations:
  - b.1) Set all the approximation coefficients as 0’s.
  - b.2) Set the first level detail coefficients as 0’s.
  - b.3) Set the second level detail coefficients as 0’s.**Note: Please solve the above three questions without using any Matlab built-in function.** Display the reconstructed image for each of the above three operations. Summarize the reasons for current appearance of the reconstructed image using the Matlab display function.
- c) Close all figures and all variables in the workspace.